

Mark Scheme 4730
June 2006

1	(i)	M1		For using $I = \Delta(mv)$ in the direction of the original motion (or equivalent from use of relevant vector diagram).
	$20\cos\theta = 0.4 \times 25$ Direction at angle 120° to original motion	A1 A1	3	Accept $\theta = 60^\circ$ with θ correctly identified.
	(ii)	M1		For using $I = \Delta(mv)$ perp. to direction of the original motion (or equivalent from use of relevant vector diagram).
	$20\sin 60^\circ = 0.4v$ Speed is 43.3 ms^{-1}	A1ft A1	3	
2		M1		For applying Newton's 2 nd Law.
	$2v(dv/dx) = -(2v + 3v^2)$	M1 A1		For using $a = v(dv/dx)$.
	$2/3\ln(2 + 3v) = -x \quad (+C)$	M1		For separating variables and attempting to integrate.
	$[2/3\ln 14 = C]$	A1ft		ft absence of minus sign,
	$[2/3\ln 2 = -x + 2/3\ln 14]$	M1		For using $v(0) = 4$.
	Comes to rest after travelling 1.30m	M1	8	For attempting to solve $v(x) = 0$ for x . AG

3	(i)	M1	For taking moments about C for the whole structure.
	$1.4R = 0.35 \times 360 + 1.05 \times 200$	A1	
	Magnitude is 240N	A1	AG
		M1	For taking moments about A for the rod AB.
	$0.7 \times 240 = 0.35 \times 200 + 1.05T$	A1	
	Tension is 93.3N	A1	6

	OR		
	(i)	M1	For taking moments about A for AB and AC.
	$0.7R_B = 70 + 1.05T$ and	A1	
	$0.7R_C = 126 +$		
	$1.05T$	M1	For eliminating T or for adding the equations, and then using $R_B + R_C = 560$.
	$0.7(560 - R_B) - 0.7R_B = 126 - 70$ or	A1	For a correct equation in R_B only or T only
	$0.7 \times 560 = 70 + 126 +$		
	$2.1T$		
	Magnitude is 240N	A1	AG
	Tension is 93.3N	A1	6

	(ii)	B1ft	
	Horizontal component is 93.3 N to the left		
	$Y = 240 - 200$	M1	For resolving forces vertically.
	Vertical component is 40 N downwards	A1	3

4	(i)	M1		For using Newton's 2 nd Law perp. to string with $a = L\ddot{\theta}$.
		A1		
		B1		
		M1		For using $T = 2\pi/\omega$ and $k = \omega^2$ or $T = 2\pi\sqrt{L/g}$ for simple pendulum.
	Period is 3.14s.	A1	5	AG
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	(ii)	M1		For using $\dot{\theta}^2 = \omega^2(\theta_0^2 - \theta^2)$ or the principle of conservation of energy
	$\dot{\theta}^2 = 4(0.1^2 - 0.06^2)$ or $\frac{1}{2}m(2.45\dot{\theta})^2 = 2.45mg(\cos 0.06 - \cos 0.1)$ Angular speed is 0.16 rad s^{-1} .	A1		
		A1	3	(0.1599... from energy method)
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	OR (in the case for which (iii) is attempted before (ii))			
	(ii) [$\dot{\theta} = -0.2\sin 2t$] $\dot{\theta} = -0.2\sin(2 \times 0.464)$ Angular speed is 0.16 rad s^{-1} .	M1 A1ft A1		For using $\dot{\theta} = d(\text{Acos } \omega t)/dt$
			3	
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	(iii)	M1		For using $\theta = \text{Acos } \omega t$ or $\text{Asin}(\pi/2 - \omega t)$ or for using $\theta = \text{Asin } \omega t$ and $T = t_{0.1} - t_{0.06}$ ft angular displacement of 0.04 instead of 0.06
	$0.06 = 0.1\cos 2t$ or $0.1\sin(\pi/2 - 2t)$ or $2T = \pi/2 - \sin^{-1}0.6$ Time taken is 0.464s	A1ft A1		
			3	

5		M1		Σmv conserved in i direction.	
	$2 \times 12 \cos 60^\circ - 3 \times 8 = 2a + 3b$	A1			
		M1		For using NEL	
	For LHS of equation below	A1			
	$0.5(12 \cos 60^\circ + 8) = b - a$	A1		Complete equation with signs of a and b consistent with previous equation.	
		M1		For eliminating a or b .	
	Speed of B is 0.4ms^{-1} in i direction	A1			
$a = -6.6$	A1				
Component of A 's velocity in j direction is	B1		May be shown on diagram or implied in subsequent work.		
$12 \sin 60^\circ$					
Speed of A is 12.3ms^{-1}	B1ft				
	M1		For using $\theta = \tan^{-1}(\text{jcomp}/\pm \text{i comp})$		
Direction is at 122.4° to the i direction	A1ft	1 2	Accept $\theta = 57.6^\circ$ with θ correctly identified.		
6	(i)	T = $1470x/30$	B1		
		[$49x = 70 \times 9.8$]	M1	For using $T = mg$	
		$x = 14$	A1		
		Distance fallen is 44m	A1ft	4	
	(ii)	PE loss = $70g(30 + 14)$	B1ft		
		EE gain = $1470 \times 14^2 / (2 \times 30)$	B1ft		
		[$\frac{1}{2} 70v^2 = 30184 - 4802$]	M1		For a linear equation with terms representing KE, PE and EE changes.
		Speed is 26.9ms^{-1}	A1	4	AG
	OR				
	(ii)	[$0.5 v^2 = 14g - 68.6 + 30g$]	M1		For using Newton's 2 nd law ($vdv/dx = g - 0.7x$), integrating ($0.5 v^2 = gx - 0.35x^2 + k$), using $v(0)^2 = 60g \rightarrow k = 30g$, and substituting $x = 14$.
	For $14g + 30g$	B1ft			
	For ∓ 68.6	B1ft		Accept in unsimplified form.	
	Speed is 26.9ms^{-1}	A1	4	AG	
(iii)	PE loss = $70g(30 + x)$	B1ft			
	EE gain = $1470x^2 / (2 \times 30)$	B1ft			
	[$x^2 - 28x - 840 = 0$]	M1		For using PE loss = KE gain to obtain a 3 term quadratic equation.	
	Extension is 46.2m	A1	4		
OR					
(iii)		M1		For identifying SHM with $n^2 =$	
				$1470 / (70 \times 30)$	
		M1		For using $v_{\text{max}} = An$	
	$A = 26.9 / \sqrt{0.7}$	A1			
	Extension is 46.2m	A1	4		

7	(i)	$\frac{1}{2} 0.3v^2 + \frac{1}{2} 0.4v^2$	B1			
		$\pm 0.3g(0.6\sin\theta)$	B1			
		$\pm 0.4g(0.6\theta)$	B1			
		$[0.35v^2 = 2.352\theta - 1.764\sin\theta]$	M1		For using the principle of conservation of energy.	
		$v^2 = 6.72\theta - 5.04\sin\theta$	A1	5	AG	
	(ii)			M1		For applying Newton's 2 nd Law radially to P and using $a = v^2/r$
		$0.3(v^2/0.6) = 0.3g\sin\theta - R$	A1			
		$[\frac{1}{2}(6.72\theta - 5.04\sin\theta) =$	M1			For substituting for v^2 .
		$0.3g\sin\theta - R]$				
		Magnitude is $(5.46\sin\theta - 3.36\theta)N$	A1			AG
(iii)			M1		For using $dR/d\theta = 0$	
	$[5.46\cos\theta - 3.36 = 0]$	M1				
	Value of θ is 0.908	A1	6			
	(iii) $[T - 0.3g\cos\theta = 0.3a]$	M1			For applying Newton's 2 nd Law tangentially to P	
	$[0.4g - T = 0.4a]$	M1			For applying Newton's 2 nd Law to Q [If $0.4g - 0.3g\cos\theta = 0.3a$ is seen, assume this derives from $T - 0.3g\cos\theta = 0.3a$ M1 and $T = 0.4g$ M0]	
	Component is $5.6 - 4.2\cos\theta$	A1	3			
OR	(iii) $0.4g - 0.3g\cos\theta = (0.3 + 0.4)a$	B2				
	Component is $5.6 - 4.2\cos\theta$	B1	3			
OR	(iii) $[2v(dv/d\theta) = 6.72 - 5.04\cos\theta]$	M1			For differentiating v^2 (from (i)) w.r.t. θ	
	$2(0.6a) = 6.72 - 5.04\cos\theta$	M1			For using $v(dv/d\theta) = ar$	
	Component is $5.6 - 4.2\cos\theta$	A1	3			